

Raniganj Girls' College

Department of Mathematics

SEM-vi, Mathematics(Hons)

Paper : DSE Mechanics III(Statics & Hydrostatics)

F.M:-40

1. Answer any five questions :- 5*1=5
 - a. Write down the necessary condition of equilibrium.
 - b. What is the relation between volume and temperature in an adiabatic change ?
 - c. What is an example of an adiabatic process?
 - d. What is the fundamental equation of Hydrostatics ?
 - e. Write down the first law of thermodynamics.
 - f. Write the dimension of buoyancy.
 - g. What is the vector equation of Poinsot's central axis?
 - h. What is the dimension of pressure?
2. Answer any five questions:- 5*2=10
 - a. What is pitch?
 - b. Write down Boyle's law and Charles's law.
 - c. What is hydrostatics equilibrium?
 - d. Define catenary of uniform strength.
 - e. What do you mean by virtual work ?
 - f. Write down the general Cartesian equation of Equilibrium of a string under coplanar forces.
 - g. What is Poinsot's central axis?
 - h. Is there any difference between tension and thrust ?
3. Answer any three questions:- 3*5=15
 - a. For equal heavy rods (uniform) are freely jointed so as to form a rhombus which freely suspended by one angular point and the middle points of the two upper rods are connected by a light rod so that the rhombus can not collapse. Prove that tension on this light rod $4wtan\alpha$, where w is the weight of each rod and 2α is the angle of rhombus of the point of suspension.
 - b. A square frame work formed at heavy uniform rods of equal weight w jointed together is hung up by one corner. A weight w is suspended from each of the three lower corners and the shape of the square is preserved by a light rod along the horizontal diagonal. Find the thrust of the light rod.
 - c. Prove that $C_p - C_v = R$. (usual notations)
 - d. Prove that $pV^\gamma = \text{constant}$. (usual notations)
 - e. A rhombus ABCD is formed of four equal uniform rods freely joined together and suspended from the point A; it is kept in position by a light rod joining the mid points of

BA and AD. If T be the thrust in this rod and w the weight of the rhombus , prove that $T = w \tan \frac{A}{2}$.

4. Answer any one question:-

1*10=10

a. (i) Prove that any system of coplanar forces acting on a rigid body can be reduced to a single resultant force acting at any arbitrary point in the plane, together with a single resultant couple of moment which is equal to the algebraic sum of the moment of the given forces about that arbitrary point.

(ii) OA,OB,OC are the edges of a cube and OO^1, AA^1, BB^1, CC^1 are in diagonal; along BC^1, CA^1, AB^1 and OO^1 act forces equal to X,Y,Z and R respectively, show that they are equivalent to a single resultant if $\sqrt{3} (YZ+ZX+XY)+R(X+Y+Z)=0$.

b. (i) A force p acts along the axis of x and another force np acts along a generator of the cylinder $x^2+y^2=a^2$; show that the central axis lies on the cylinder $n^2(nx-z)^2 + (1+n^2)^2y^2 = n^4a^2$.

(ii) A telegraph wire stretched between two poles at a distance 'a' feet apart, sags 'n' feet in the middle; prove that the tension at the ends is approximately $w(\frac{a^2}{8n} + \frac{7}{6}n)$.